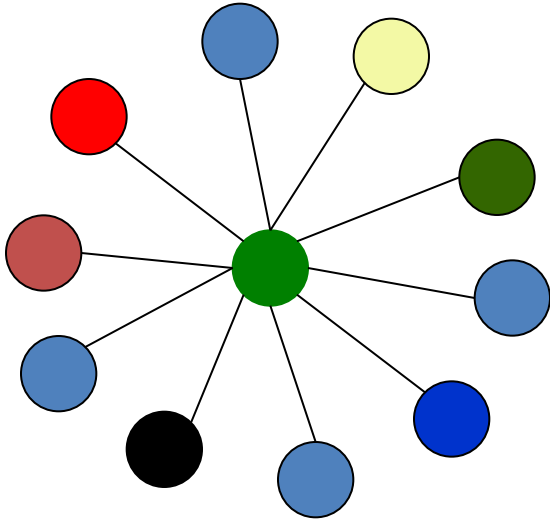


# Economics of Networks III



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**2017 Winter School  
Delhi School of Economics**

## Communities in society

- We study interaction between communities with conflicting views on norms, e.g., language, dress, hospitality, food and diet.
- Diversity is valued but at the same time it is also viewed as a major social challenge.
- **Aim:** understand mechanisms that shape conformism vs diversity.

## Case for diversity

- Valued: diversity respects individual preferences and values. This is important in itself in a liberal society. Diversity brings variety and that may have value in itself.
- Diversity may also have instrumental value as it potentially brings different perspectives into play and that may facilitate best practice across a range of societal contexts.

## Challenges to diversity

- Challenge: contemporary politics in many parts of the world.
- Brexit is at least partly driven by recent immigration and a fear of further large scale immigration.
- Immigrant ghettos in European cities are viewed as a social and economic problem.
- Traditional argument: communities choose segregation over integration.

## In this lecture

- We study coordination problem with many individuals.
- Individuals gain payoffs by coordinating with others.
- There are two actions and individuals differ on preferred action.
- A battle of sexes in a group setting..
- Question: when will a minority conform with the majority or and when will it go its own separate way?

## Background

- Coordination problems: Schelling (1960), Gauthier (1972).
- Anderlini and Ianni (1996), Blume (1993), Ellison (1993), Goyal and Janssen (1997): interaction structure matters for coordination.
- Early work with simple networks: lattices and rings.
- Goyal and Vega-Redondo (2005) Jackson and Watts (2002): players choose *networks* and then play a coordination game.
- Advani and Reich (2015), Ellwardt et al. (2016): introduce heterogeneous preferences.

## Framework: Social Coordination with Heterogenous Preferences

- Two types of individuals and two actions
- Everyone prefers to coordinate on same action
- Type A prefers action  $a$ , type B prefers action  $b$
- Individuals choose actions simultaneously
- Two settings: exogenous interaction vs. choose links and action
- Question: what are the mechanisms that facilitate conformism and diversity?

# Model

Goyal, Hernandez, Martinez, Moisan, Munoz, Sanchez 2017

- Players:  $N = \{1, 2, \dots, n\}$  with  $n \geq 3$ .
- Two types:  $\theta_i \in \{a, b\}$ .
- Two stage game: first choose link proposals and then choose actions.
- First stage: every player proposes links to everyone else. Links are binary,  $g_{ij} \in \{0, 1\}$ .
- Define  $\bar{g}_{ij} = g_{ij}g_{ji}$ . Set of undirected networks is  $\bar{g}$ .
- Second stage: every player  $i$  chooses action  $x_i : \bar{g} \rightarrow \{a, b\}$ .
- Neighbours:  $N_i(\bar{g}) = \{j \in N : \bar{g}_{ij} = 1\}$ .



## Model

- Following Ellwardt et al (2016), the payoff to player  $i$  from  $\mathbf{s} = (x, g) = (x_1, \dots, x_n, g_1, \dots, g_n)$ :

$$u_i(\theta_i, x, \bar{g}) = \lambda_{x_i(\bar{g})}^{\theta_i} \left( 1 + \sum_{j \in N_i(\bar{g})} I_{\{x_i(\bar{g})=x_j(\bar{g})\}} \right) - |N_i(\bar{g})|k \quad (1)$$

$I_{x_j=x_i}$  = indicator function for  $i$ 's neighbour  $j$  who choose same action as  $i$ .

- $\lambda_{x_i(\bar{g})}^{\theta_i} = \alpha$  if  $x_i(\bar{g}) = \theta_i$ ;  $\lambda_{x_i(\bar{g})}^{\theta_i} = \beta$  if  $x_i(\bar{g}) \neq \theta_i$ .
- Assume  $\alpha > \beta$  and  $k \in \mathbb{R}$ . Interesting case:  $\beta > k$

## Proposition: Exogenous Interaction

Let  $\chi_i(\bar{g}) = \{j \in N_i(\bar{g}) : x_j^* = \theta_i\}$ .

Given an undirected network  $\bar{g}$ , action profile  $x^*$  is a Nash equilibrium if and only if for any  $i \in N$ :

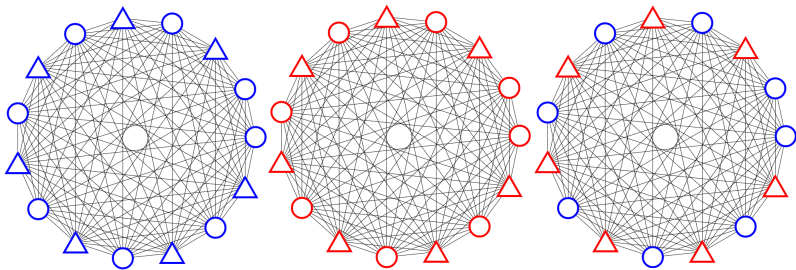
$$x_i^* \begin{cases} = \theta_i & \text{if } |\chi_i(\bar{g})| > \frac{\beta}{\alpha+\beta} |N_i(\bar{g})| - \frac{\alpha-\beta}{\alpha+\beta} \\ \neq \theta_i & \text{if } |\chi_i(\bar{g})| < \frac{\beta}{\alpha+\beta} |N_i(\bar{g})| - \frac{\alpha-\beta}{\alpha+\beta} \end{cases}$$

## Example: Complete Network

Let  $N_O$  and  $N_\Delta$  be the sets of players who prefer  $b$  and  $r$ .

Fix a complete network  $\bar{g}$ . In Nash equilibrium  $x^*$ :

- **Conformity**  $x_i^* = x_j^* \in \{b, r\}$  for all  $i, j \in N$  if  $n \geq \frac{\alpha}{\beta}$ .
- **Diversity**  $x_i^* = \theta_i$  for all  $i \in N$  if  $|N_O|, |N_\Delta| \geq \frac{\beta(n+1)}{\alpha+\beta}$ .

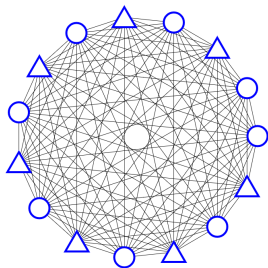


## Proposition: Efficient Outcome in Complete Network

Let aggregate welfare be given by sum of utility of all players.

A socially efficient outcome  $x$  entails all players conforming to the majority's preferred action.

$\Rightarrow$  For every  $i, j \in N$ ,  $x_i = x_j = \arg \max_{c \in A} |\{k \in N : \theta_k = c\}|$



## Endogenous Interaction: Pairwise stable Networks

A network-action pair  $(\bar{g}, x(\bar{g}))$  is pairwise stable if:

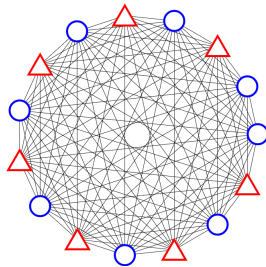
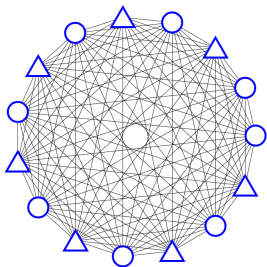
- $x(\bar{g})$  is an equilibrium action profile given network  $\bar{g}$ .
- for every  $\bar{g}_{ij} = 1$ ,  $u_i(x, \bar{g}) \geq u_i(x, \bar{g} - \bar{g}_{ij})$  and  $u_j(x, \bar{g}) \geq u_j(x, \bar{g} - \bar{g}_{ij})$ , where  $x$  is such that  $x_{-ij}(\bar{g} - \bar{g}_{ij}) = x_{-ij}(\bar{g})$ , and  $x_l \in \arg \max_{x'_l \in X_l} u_l(\theta_l, x'_l, x_{-l}, \bar{g} - \bar{g}_{ij})$  for  $l \in \{i, j\}$ .
- for every  $\bar{g}_{ij} = 0$ ,  $u_i(x, \bar{g}) \geq u_i(x, \bar{g} + \bar{g}_{ij})$  or  $u_j(x, \bar{g}) \geq u_j(x, \bar{g} + \bar{g}_{ij})$  where  $x$  is such that  $x_{-ij}(\bar{g} + \bar{g}_{ij}) = x_{-ij}(\bar{g})$ , and  $x_l \in \arg \max_{x'_l \in X_l} u_l(\theta_l, x'_l, x_{-l}, \bar{g} + \bar{g}_{ij})$  for  $l \in \{i, j\}$ .

# Pairwise Stable Networks: Partial Characterization

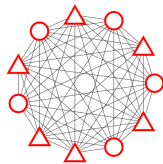
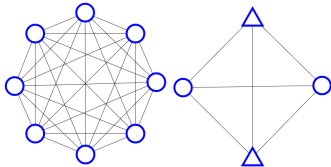
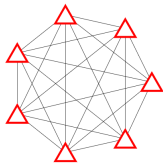
Suppose  $k = 0$ . In pairwise stable equilibrium  $s^* = (\bar{g}^*, x^*)$ , outcomes include

- (i) Full Integration with Conformity.
- (ii) Full Segregation with diversity.
- (iii) Complete integration with diversity.

## Pairwise Stable Networks: Integration



# Pairwise Stable Networks: Segregation







# Summary

- Exogenous complete network:
  1. Multiple equilibria: (1) conformity and (2) diversity
  2. Types relevant only in diversity equilibrium
  3. Conformity is aggregate welfare maximizing
- Endogenous setting:
  1. Multiple equilibria: (1) integration with conformity, (2) segregation with diversity (3) Integration with diversity
  2. Integration with conformity is aggregate welfare maximizing
- How does endogenous linking shape equilibrium selection?

# Design

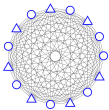
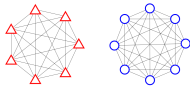
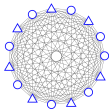
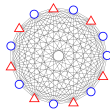
## Experimental variables:

- Freedom of linking
  - ⇒ Exogenous vs. endogenous network
- Risk of linking
  - ⇒ Different cost of linking with someone who mis-coordinate



## Some predictions

$|N_O| = 8$  and  $|N_\Delta| = 7$ :

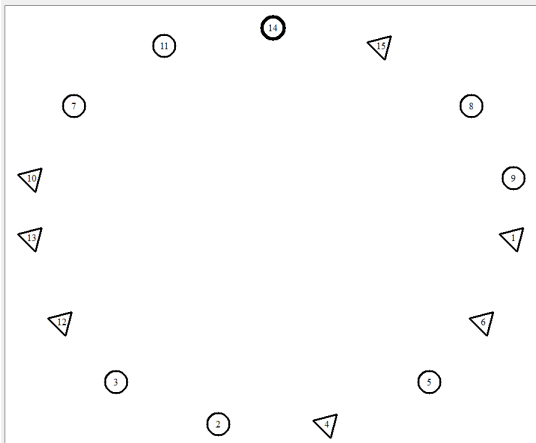
Player type	Equilibrium Payoffs			
	Endogenous		Exogenous	
				
Minority ( $\Delta$ )	$30+k$	$28+k$	30	28
Majority (O)	$60+k$	$32+k$	60	32

## Further Details

- Experiment run at **LINEEX** (University of Valencia)
- 6 groups / treatment
- Sessions of 3 groups (2 sessions / treatment)
- 5 trial rounds (no payoff) + 20 rounds (actual game)
- Fixed group matching
- Conversion rate: 50 points = 1 euro
- Mean earnings = 18 euros
- Mean duration = 100 mins
- Demographics: age: from 18 to 30; 42% male, 58% female

# Stage 1 (round 1)

Your group, formed by 8 circles and 7 triangles:



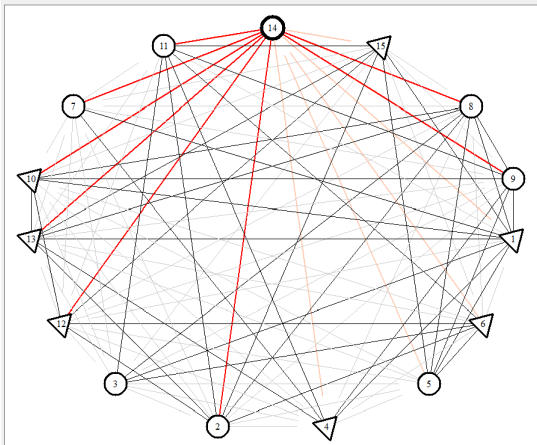
## PROPOSALS

Check the participant(s) to whom you want to propose a connection

- 1
- 2
- 3
- 4
- 5
- 6
- 7
- 8
- 9
- 10
- 11
- 12
- 13
- 15

# Stage 2

Resulting network:



## ACTION

Choose an action

- Up
- Down

Round 1/20

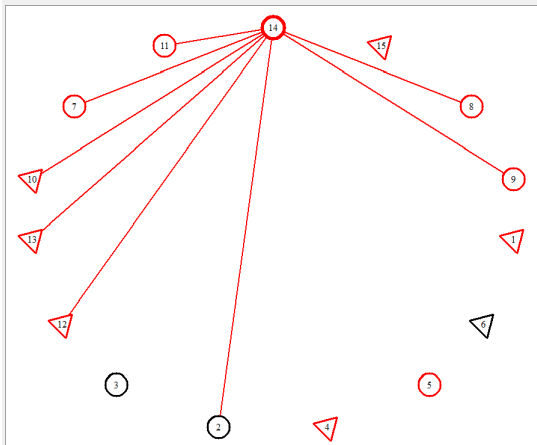
You are player **14**

Continue



# Feedback stage 2

Your connections:



## RESULTS

You chose action **Up**.  
You have coordinated with **7**  
of your **8** connections.

You win:  
4 points (coordination with yourself) +  
4 \* 7 = 28 points (coordinations)  
Total: 32 points

In this Round you obtain:  
**32 points**

The participants with red border chose the same action as you.

Round 1/20

You are player **14**

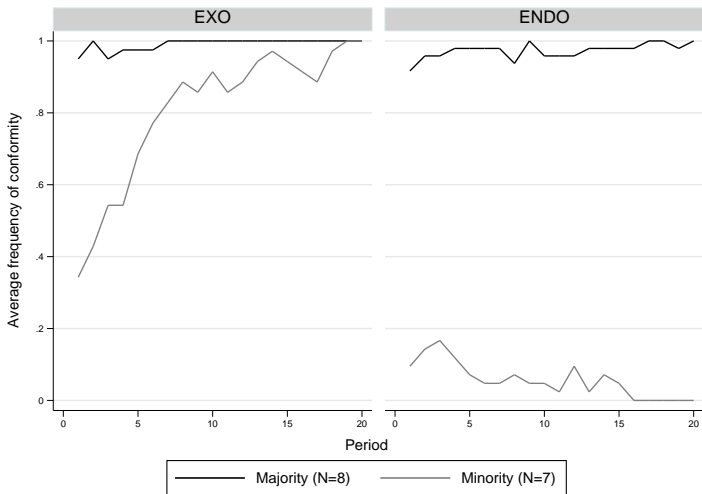
OK

# Conformity: Exogenous versus endogenous links

⇒ Animations

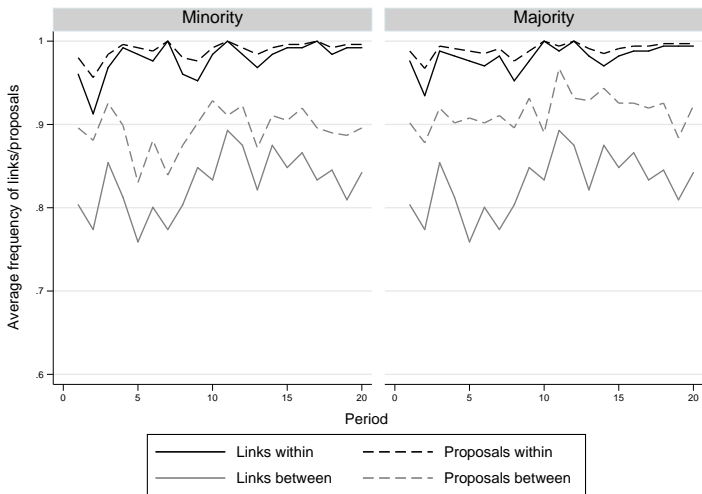
# Conformity: Exogenous versus endogenous links

⇒ Animations



# Connectivity: FREE Links

⇒ Animations



## Results: summary

- Exogenous complete network:
  - Conformity on majority's preferred action.
  - Efficient outcome.
- Endogenous linking:
  - Very dense network and diversity in actions
  - Segregation across communities (with positive linking costs)
  - Large welfare losses

## Hypothesis: The Network as a Signal

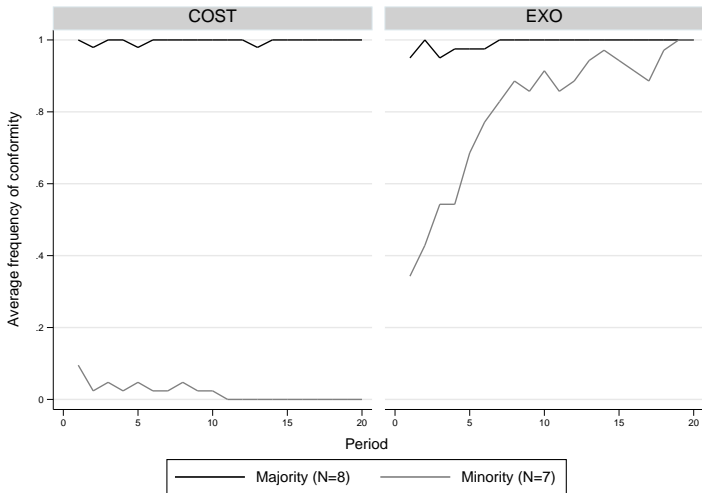
- Coordination problem is very complicated
- Links are a route to signal intention on play
- Players will be willing to pay for the signal
- Positive cost link: proposal to other type signals intention to coordinate
- Negative cost link: not proposing to other type signals intention to play own preferred action.

# Cost Treatment

⇒ Animations

# Cost Treatment

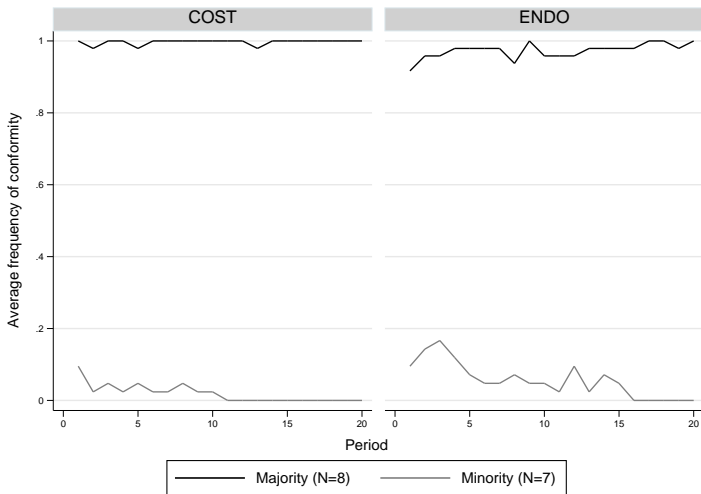
⇒ Animations





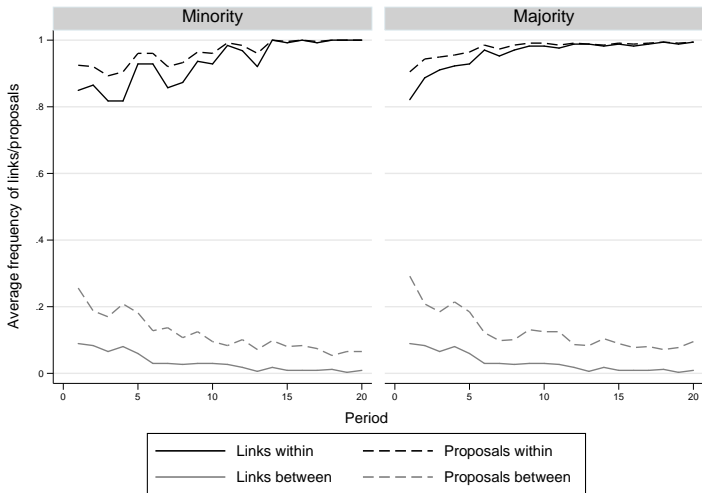
# Cost Treatment

⇒ Animations



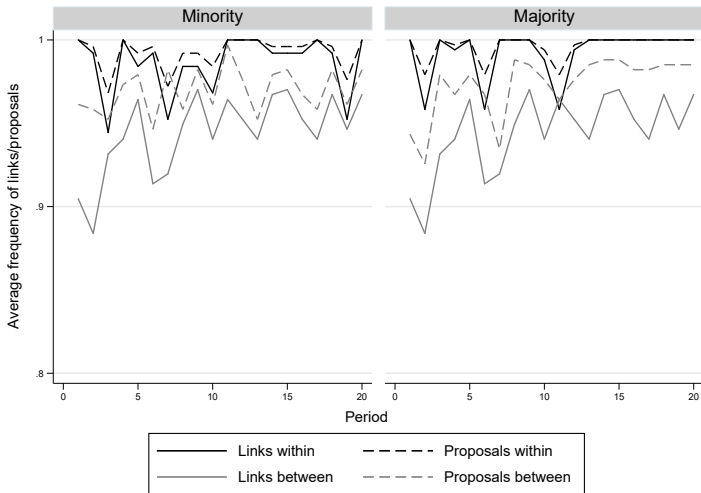
# Connectivity

⇒ Animations



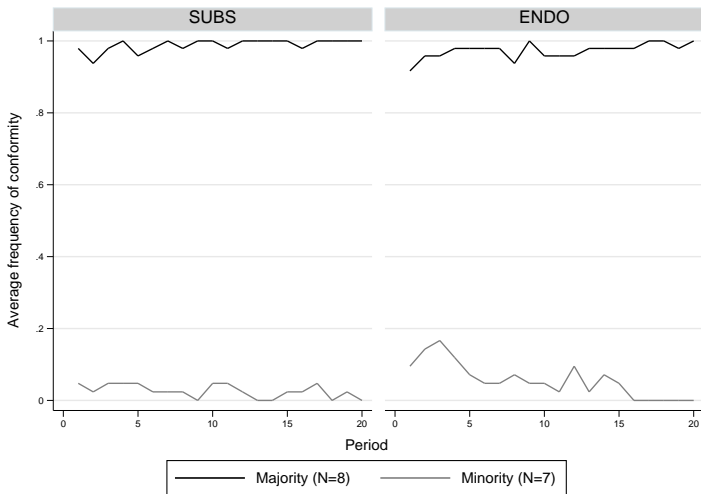
# The Negative Cost Treatment: SUBSIDY

⇒ Animations



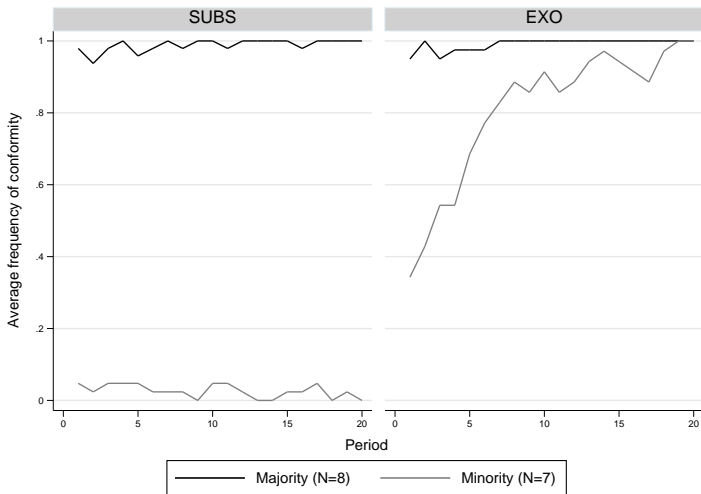
# Diversity: Negative cost links vs Free links

⇒ Animations



# Diversity: Negative cost links vs Exogenous

⇒ Animations



# Regression on linking and conformity

```
.          xtreg net_conform_min_norm rate_links_group period, cl(treat)

Random-effects GLS regression              Number of obs   =       600
Group variable: group                      Number of groups  =       30

R-sq:                                      Obs per group:
      within = 0.1221                       min =           20
      between = 0.1048                      avg =          20.0
      overall = 0.1031                      max =           20

                                           Wald chi2(2)     =       31.73
corr(u_i, X) = 0 (assumed)                Prob > chi2      =       0.0000
```

(Std. Err. adjusted for 5 clusters in treat)

	Robust				
net_conform_mi~m	Coef.	Std. Err.	z	P> z	[95% Conf. Interval]
rate_links_group	.6874037	.3045453	2.26	0.024	.090506 1.284301
period	-.0004691	.0055491	-0.08	0.933	-.0113452 .010407
_cons	-.1653395	.1737085	-0.95	0.341	-.505802 .1751229
sigma_u	.46032431				
sigma_e	.19024515				
rho	.85411354	(fraction of variance due to u_i)			

## Concluding remarks

- Diversity is valued but it also poses a major challenge.
- We study interaction between communities that have differing views.
- Develop a model: coordination with heterogeneous preferences.
- Theory is permissive: variety of outcomes possible in equilibrium.
- Study mechanisms for equilibrium selection.
- Hypothesis: networks are a signal for intentions in the coordination game.

## Main Findings

- Allowing people to choose links leads to diversity
  - With exogenous complete network: conformism
  - With endogenous free links: close to full integration but diversity.
- Links are a signalling mechanism
  - With positive cost: segregation and diversity.
  - With negative cost: high integration and diversity.